The Formation of Peer Groups in the Pricing Process of Privately Held Businesses: Can Firm Size Serve as a Selection Criterion? Empirical Evidence from Europe

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Abstract

Business valuation professionals consider transaction multiples as an accurate method to price privately held businesses. The formation of comparable peer groups is crucial for this method. A problem arises when it comes to identify adequate peer group selection criteria. For practicability reasons industry classification is widely used but recent literature indicates that the comparability of peer groups could be increased by adding firm size as selection criterion. This paper aims at analyzing the effect of firm size as additional peer group selection criterion. More specifically, it focuses on the effect of firm size on the reliability of transaction multiples which are used to estimate transaction prices for privately held businesses. Based on literature, real transaction price data from Europe is applied to verify the influence of firm size. The results indicate the highest reliability of transaction multiples when combining industry classification with firm size in the peer group formation process.

Keywords: Peer Group Selection Criteria, Transaction Multiples, Privately Held Businesses, Industry Classification, Size Effect, Business Valuation, Transaction Price

1 Introduction

In a transaction of a privately held business, acquirer and vendor finally have to agree on the transaction price to close the deal. One common method to generate indications on transaction prices for privately held businesses is the Recent Acquisitions/Transaction Method (RAM/RTM), a specific method of the Market Approach (Pratt, 2005). In the RAM/RTM the indication on the transaction price is generated through a comparison with the recently realized transaction prices of comparable (i.e. similar) businesses. This means that the transaction price can be derived from the prices at which entire businesses or operating units of businesses have been sold or the prices at which significant interests in businesses have changed hands (Pratt and Niculita, 2008). Therefore, the businesses that are compared and used as surrogates must be comparable to the appraisal subject, the "target business" (Pratt, Reilly and Schweihs, 1998). As a result of this comparison a "transaction multiple "can be calculated. From the transaction multiples an individual transaction price for the target business as a multiple of a specific financial value driver can then be derived (Liu, Nissim and Thomas, 2002). In practice business appraisers mainly use financial value drivers as "sales", "earnings before interest and taxes" (EBIT) and/or "earnings before interest and taxes, depreciation and amortization" (EBITDA) to value privately held businesses by deploying transaction multiples (Pratt, 2005; Mellen and Evans, 2010; Trugman, 2012).

The main problem during the pricing process of privately held businesses is to assess the comparability between the target business and the comparable businesses. To be able to do this it is necessary to choose the relevant parameters to identify comparable businesses for the peer group. Business appraisers commonly use two different methods to overcome this problem and to find the "right" peer group with the best fit. The first is based on an analytical selection process (Damodaran, 2010; Trugman, 2012). The goal of applying this method is to add only a few – but therefore highly comparable businesses –to the peer group. The second method, the "Direct Market Data Method" (Miles, 1999), adds all businesses of the specific industry to the peer group. This method only focuses on the industry sector the business belongs to(either the target business or the comparable business). Therefore, the relevant parameters to identify comparable businesses are reduced only to one parameter, the industry classification.

The identification of the best fit of a peer group is highly relevant because the quality, the representativeness, the homogeneity and hence the reliability of the transaction multiple is highly dependent on the comparability of the businesses. To date there are no binding and internationally accepted guidelines for how to assess if a business can be considered as a comparable. The only requirement is that the businesses as a whole have to be comparable in their overall business model (Pratt and Niculita, 2008). As this is of course just a very loose framework and is therefore not very helpful in practice, business appraisers often use Porter's "Five Forces" (Porter, 2008) as a guideline in the selection process. In this process, the main selection criteria used to form a peer group are(a) the industry, (b) the size of the business, (c) the expectations of growth and profit as well as (d) the current financial situation of the business(Koller, Goedhart and Wessels, 2010; Trugman, 2012). Besides these primary selection criteria there are several other factors discussed as being worth noting in determining the comparability of the businesses. These criteria are(i) legal rights of business ownership or business equity, (ii) degree of industry specialization, (iii) past growth of sales and earnings, (iv) rate of return on the physical, functional, human capital and economic characteristics, (v) invested capital, (vi) stability of past earnings, (vii) quality of management, (viii) nature and prospects of the industry, (ix) competitive position and individual prospects of the business, (x) basic nature of the activity, (xi) general types of products produced, (xii) years in business and (xiii) geographical diversification (Houlihan and Tack, 1997; Bhojraj and Lee, 2002; Pratt, 2005; Trugman, 2012).

However, there is only little knowledge about the importance of different selection criteria and their impact on the reliability of the derived transaction multiples for privately held businesses. There is only some empirical evidence from the capital market. Henschke and Homburg (2009) found out, that using financial selection criteria to form peer groups instead of solely using the industry classification lead to statistically more reliable transaction multiples. The literature also provides checklists of criteria to be considered, but these checklists neither present a reliable ranking of the criteria nor provide sufficient evidence based on empirical data (Pratt, Reilly and Schweihs, 1998). Furthermore, no procedure for selecting the comparable businesses neither for available selection criteria from the United States of America (Trugman, 2012) nor for selection criteria from European countries is reported. Against this background, the analysis presented in this paper aims at answering the following research question:

"Does firm size as a peer group selection criterion have an influence on the reliability of transaction multiples, which are used to estimate transaction prices for privately held businesses?"

To answer this question this paper is structured as follows. Section 2 presents the theoretical background. The materials and methods section 3 gives an overview of the sample, the data source as well as the method used to answer the research question. The results and discussion section 4 focuses on the following key findings: the results of the data analysis (i) increase the body of knowledge on primary selection criteria in the context of defining a peer group of comparable businesses and (ii) provide practical guidelines for business appraisers to help them disclosing and documenting all their criteria used in the selection process to make their decisions as reproducible and reliable as possible. The paper concludes with the final section 5 that gives some ideas for further research and addresses the limitations of the conducted study.

2 Theoretical Background

2.1 Transaction price versus value of a business

In general, the transaction price of businesses has to be distinguished strictly from its value. The price shows the amount of money that is bargained and finally paid in the transaction and therefore represents the value expressed as an amount of money that is given for the achievement of control over the business. The value of the business, however, represents only a potential price. It just shows the price at which the business should be transacted in order to keep the property of either the acquirer or the vendor in a steady state, but it fails to say whether the business is finally really transacted at that specific price.

2.2 Transaction multiples and their use in RAM/RTM to estimate an individual transaction price

Transaction multiples indicate the transaction price of a target business on the basis of a comparison with recently realized prices of comparable businesses. The price of the target is therefore generated as a result of successfully closed transactions on the "free" Mergers and Acquisitions (M&A) market. The starting point of this technique is the basic thought of Jevons' "Law of One Price" that "similar assets should sell at similar prices". Consequently, the RAM/RTM follows the assumption that businesses that are comparable in terms of their essential economic parameters should also be transacted at the same prices.

The RAM/RTM is a highly market-oriented method that is based on already existing prices in the M&A market and therefore focuses on all integrated market information. The use of this method is therefore an expression of trusting in the functionality and the efficiency of the market mechanism (Herrmann and Richter, 2003; Pratt and Niculita, 2008). The individual transaction price of the target is technically calculated by a multiplication of the known financial value driver of the target business (that must be a representative indicator of its economic performance) with the multiple derived from the comparable businesses. This multiple is the quotient of the known transaction prices of the comparable businesses and their also known value drivers (Damodaran, 2012). In other words, the multiple represents the number of times the value driver was paid. By multiplying the multiple with the value driver of the target business, this relationship between the price and the value drivers of the comparable businesses is transferred directly to the target business. In addition to that it is to be assumed that there exists a linear relationship between the transaction price and the value driver (that means, for example, that the double value driver causes no more or less than the double value of the business). All components of the economic performance that have no influence on the value driver will not be regarded and consequently not be transferred to the target business. For these factors it is assumed that they are either non-existent or equal. Therefore, the value driver must contain all factors that have an influence on the economic performance of the target business.

2.3 Types of transaction multiples

Transaction multiples reflect the market price of the total capital and of ownership interests and therefore lead to the Deal Enterprise Value (DEV) of the business. The big advantage of DEV transaction multiples is their independency from the structure of financing, especially the debt to equity ratio. In the literature various types of transaction multiples can be found, differing on the regarded factors that have an influence on the transaction price. As mentioned in section 1, sales, EBIT and EBITDA are widely used value drivers. The basic and pragmatic reason to use them is that a statistically sufficient amount of information concerning the transaction data, especially for small and midsize businesses, is recorded and therefore available. As a result, the common DEV-Multiples used are the DEV/Sales, the DEV/EBITDA and the DEV/EBIT Multiple (Pratt, Reilly and Schweihs, 1998; Schwetzler, 2010; Trugman, 2012).

2.3.1"DEV/Sales" transaction multiple

The DEV/Sales transaction multiple assumes that all businesses have an identical economic growth rate, identical investing quotes and identical profit margins. Its advantages are: (i) it is the most consistent multiple concerning the accounting policy and different tax and accounting systems, (ii) it can also be used for businesses with unknown or negative profits, (iii)it is usually less volatile than the profit multiples over the years,(iv)it cannot become negative and therefore the otherwise enforced elimination of negative transaction multiples cannot skew the averaged transaction multiple and (v)it is relatively lower in its absolute amount. Its disadvantages are, besides the above mentioned assumptions of identical economic parameters that the overall economic performance of the business and especially the structure of costs are not taken into consideration.

2.3.2"DEV/EBITDA" transaction multiple

The DEV/EBITDA transaction multiple represents the purely operative performance of the business in view of its profit and offers various advantages: (i) it enables the appraiser to take into consideration the economic performance of the business, (ii) it is closely related to the cash flow (differences only occur according to net investments and changes in the working capital), (iii) it is independent from the policy of depreciation and the financing of the assets and (iv)it is independent from the type of economic growth (internal or external). Its disadvantages are the disregarding of different policies of depreciation and different capital structures between businesses and the enforcement of eliminating negative transaction multiples that as a result may skew the averaged transaction multiple.

2.3.3"DEV/EBIT" transaction multiple

The DEV/EBIT transaction multiple shows the performance of the business in view of the profit before, i. e. independent of all financing activities. Therefore, it takes into consideration all differences between businesses concerning their policy of depreciation and economic growth. The disadvantages are the disregarding of different capital structures between businesses and again the enforcement of eliminating negative transaction multiples that as a result may skew the averaged transaction multiple.

3 Materials and Method

The data used is extracted from the M&A database ZEPHYR. The ZEPHYR database gives the largest number of available transaction data for Europe. The transactions taken into consideration fulfill the following four criteria: (i) The headquarters of the transacted businesses are situated in the specified region. (ii) The transaction (merger or acquisition) was closed within the time period January 1st 2007 to December 31st 2011. (iii) The transaction either refers to the transfer of a majority stake and therefore enables the acquirer to control the target business directly or the transaction refers to the transfer of a minority stake and this stake gives the acquirer a majority stake in combination with the already existing minority stake; the transaction of minority stakes (that not even give the acquirer a majority interest in combination with eventually already existing minority stakes) are transferred to the level of a majority stake by adding a control premium on the basis of the Mergerstat/Shannon Pratt's Control Premium StudyTM. This study considers the median premium without negatives (Pratt, 2005; Pratt, 2009; Pratt and Niculita, 2008; Abrams 2010). The last criterion is that(iv) the EBITDA or the EBIT have to be positive. The calculated transaction multiples therefore reflect the DEV of a controlling interest of a privately held business.

The data analysis aims at answering the research question (see section 1) whether the classification of the transaction prices in view of the size of the business has an influence on the reliability of the calculated transaction multiple. In addition to that it is also examined whether the reliability of the common classification of the transaction multiples according to the industry classification can be enhanced by combining the industry classification with a size classification. To perform the data analysis, firstly, transaction multiples are calculated according to the industry classification. Following the recommendations of Schwetzler (2010), Trugman (2012) and the DVFA (2012), the results are presented in form of the median M and the harmonic meanH (see the accordingly named columns in tables 1 to 9)with eliminating outliers that may skew the average. In addition, the coefficient of variance is calculated (see also the accordingly named column in table 1 to 9). This coefficient of variance represents an indicator for the quality, the representativeness, the homogeneity and hence the reliability of the calculated transaction multiples. Secondly, the same procedure is performed according to the classification of the transacted business in view of their size following the recommended size classification of the European Union 2003/361/EG, which divides businesses into small, medium and large sized businesses. Finally, the two classifications industry and firm size are combined. Thus, the transaction multiples are calculated for each industry classified for the different firm sizes.

In order to evaluate the reliability of the derived transaction multiples, as mentioned above, the coefficient of varianceV is calculated. The lower the coefficient of variance, the higher is the reliability of the transaction multiples. The significance of the improvement of the transaction multiples is tested with a T-test at the 5% level (see the asterisk behind the coefficient of variance in tables 1 to 9). This shows the intensity of improvement of the differently classified transaction multiples compared with an aggregate calculation. The transaction multiples presented in tables 1 to 9 are calculated for all European countries that deliver a statistically sufficient number of transaction data. On the one hand, they are calculated for European aggregate and, on the other hand, for the following seven regions for which it is assumed that they are internally homogeneous although there are significant differences in the levels of the transaction multiples between them:(i) Central (Austria, Germany and Switzerland), (ii) West (Benelux countries and France), (iii) South (Italy, Portugal and Spain), (iv) North (Denmark, Finland, Iceland, Norway and Sweden), (v) Central East (Croatia, Czech Republic, Estonia, Hungary, Latvia, Lithuania, Poland, Slovakia and Slovenia), (vi) South East (Bosnia-Herzegovina, Bulgaria, Cyprus, Greece, Romania, Serbia and Turkey) and (vii) East (Russia and the Ukraine).

4 Results and Discussion

4.1 Industry classification serving as a peer group selection criterion: its impact on the reliability of transaction multiples

In a first step the analysis was conducted for the following six industries: (i) Banking, Insurance & Financial Services, (ii) Chemicals, Petroleum, Rubber & Plastic, (iii) Computer, IT & Internet Services, (iv) Industrial, Electric & Electronic Machinery, (v) Personal, Leisure & Business Services, (vi) Retailing & Wholesaling. Additionally, the "Industry aggregate" was analyzed. This classification of the industries follows the ZEPHUS Industry classification code and represents the industries with the largest number of recorded transaction data.

The data in tables 1 to 3 (each table shows the calculation of one of the three different types of regarded transaction multiples) make evident that the classification of the transactions according to the different industries in most cases leads to a lower coefficient of variance compared to an aggregate calculation (see the "1" behind the coefficient of variance). Transaction multiples that are based on an industry classification of the comparable businesses therefore are more reliable. There is empirical evidence that justifies the industry classification as a (primary) selection criterion for the assessment of comparability of businesses. It also shows that the improvement is in many cases significant (see the asterisk behind the coefficient of variance).

Table 1: Analysis of the reliability of "DEV/Sales" transaction multiples according to industry classification serving as peer group selection criterion (using the coefficient of variance V)

European Region / Industry Classification	N	M	Н	V
Central				
Banking, Insurance & Financial Services	138	9.99	6.06	12.28^{-1}
Chemicals, Petroleum, Rubber & Plastic	111	10.33	1.37	$4.63^{-1}*$
Computer, IT & Internet Services	233	2.48	0.79	$3.08^{-1}*$
Industrial, Electric & Electronic Machinery	369	2.02	0.82	$3.83^{-1}*$
Personal, Leisure & Business Services	297	11.52	1.12	5.00 1 *
Retailing & Wholesaling	153	0.99	0.56	8.69 1 *
Industry Aggregate	1,301	3.40	0.94	15.48
West	1,501	3.70	0.51	15.70
Banking, Insurance & Financial Services	226	39.13	7.41	6.39 1 *
Chemicals, Petroleum, Rubber & Plastic	267	8.41	0.30	5.38 1 *
				6.29 ¹ *
Computer, IT & Internet Services	788 571	2.17	1.32	8.75 ¹ *
Industrial, Electric & Electronic Machinery	571	2.10	0.29	8./5 *
Personal, Leisure & Business Services	916	3.50	0.84	5.94 1 *
Retailing & Wholesaling	661	2.13	0.85	14.98 1 *
Industry Aggregate	3,429	3.01	0.96	24.59
South				. 1
Banking, Insurance & Financial Services	402	70.08	6.81	3.93 1 *
Chemicals, Petroleum, Rubber & Plastic	303	4.19	1.84	10.25
Computer, IT & Internet Services	391	4.02	1.02	5.30 1 *
Industrial, Electric & Electronic Machinery	605	6.20	1.59	7.73^{-1}
Personal, Leisure & Business Services	766	10.82	1.85	6.80^{-1}
Retailing & Wholesaling	765	3.43	1.30	15.74
Industry Aggregate	3,232	7.15	1.62	10.24
North				
Banking, Insurance & Financial Services	321	26.99	13.80	11.84
Chemicals, Petroleum, Rubber & Plastic	86	13.65	3.46	$2.65^{-1}*$
Computer, IT & Internet Services	817	4.47	0.48	4.05 1 *
Industrial, Electric & Electronic Machinery	758	7.98	3.30	4.59 1 *
Personal, Leisure & Business Services	1,049	12.45	0.18	5.85 1 *
Retailing & Wholesaling	620	14.81	0.16	6.04 1 *
Industry Aggregate	3,651	9.45	0.42	11.02
Central East	3,031	9.43	0.42	11.02
Banking, Insurance & Financial Services	197	5.45	2.05	8.49 1 *
<u> </u>			2.05	3.04 1 *
Chemicals, Petroleum, Rubber & Plastic	179 302	1.11 1.95	0.02 0.44	5.71 ¹ *
Computer, IT & Internet Services Industrial, Electric & Electronic Machinery	172	1.95	0.44	3.35 1 *
Personal, Leisure & Business Services	306	1.03	1.30	3.78 ¹ *
Retailing & Wholesaling	565	0.92	0.04	4.96 1 *
Industry Aggregate	1,721	1.46	0.04	14.22
, , , ,	1,/21	1.40	0.00	17.22
South East Parking Ingurance & Financial Services	107	6.25	0.15	$4.08^{-1}*$
Banking, Insurance & Financial Services	187	6.35	0.15	4.08 *
Chemicals, Petroleum, Rubber & Plastic	145	1.13	0.47	4.42 1 *
Computer, IT & Internet Services	84	1.97	0.69	6.30 1 *
Industrial, Electric & Electronic Machinery	159	1.63	0.00	3.72 1 *
Personal, Leisure & Business Services	214	2.50	0.59	14.48 1 *
Retailing & Wholesaling	414	1.09	0.52	7.20 1 *

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Industry Aggregate	1,203	1.52	0.01	28.28	_
East					_
	101	0.70	0.01	2 10 1 4	
Banking, Insurance & Financial Services	181	9.70	0.01	3.18 1 *	
Chemicals, Petroleum, Rubber & Plastic	219	1.19	0.26	10.29	
Computer, IT & Internet Services	91	2.19	0.85	6.28	
Industrial, Electric & Electronic Machinery	168	0.81	0.25	$2.66^{-1}*$	
Personal, Leisure & Business Services	414	1.28	0.34	5.37 1	
Retailing & Wholesaling	581	1.89	0.14	6.09^{-1}	
Industry Aggregate	1,654	1.57	0.12	6.21	
European Aggregate					_
Banking, Insurance & Financial Services	1,652	21.48	0.12	$17.00^{-1} *$	
Chemicals, Petroleum, Rubber & Plastic	1,310	2.54	0.19	8.16 1 *	
Computer, IT & Internet Services	2,706	2.85	0.67	$5.71^{-1}*$	
Industrial, Electric & Electronic Machinery	2,802	2.89	0.03	$8.09^{-1}*$	
Personal, Leisure & Business Services	3,962	4.80	0.42	38.62 1	
Retailing & Wholesaling	3,759	2.06	0.24	$11.65^{-1}*$	
Industry Aggregate	16,191	3.51	0.15	46.26	_
		-			

^{1 ...} classification according to industry leads to a lower coefficient of variance compared to an aggregate calculation

Table 2: Analysis of the reliability of "DEV/EBITDA" transaction multiples according to industry classification serving as peer group selection criterion (using the coefficient of variance V)

European Region / Industry Classification	N	M	Н	V
Central				
Banking, Insurance & Financial Services	51	17.81	7.42	$6.09^{-1}*$
Chemicals, Petroleum, Rubber & Plastic	55	15.57	12.24	$2.60^{-1} *$
Computer, IT & Internet Services	103	15.10	20.01	$1.40^{-1} *$
Industrial, Electric & Electronic Machinery	213	16.48	10.06	$4.16^{-1}*$
Personal, Leisure & Business Services	93	13.74	9.41	$2.31^{-1}*$
Retailing & Wholesaling	90	8.56	11.44	$6.68^{-1}*$
Industry Aggregate	605	14.75	10.91	15.99
West				
Banking, Insurance & Financial Services	66	23.31	11.21	5.11 1 *
Chemicals, Petroleum, Rubber & Plastic	173	35.64	90.17	3.51 1 *
Computer, IT & Internet Services	551	22.42	9.70	$5.08^{-1}*$
Industrial, Electric & Electronic Machinery	378	14.68	0.76	$10.30^{-1} *$
Personal, Leisure & Business Services	579	17.61	9.28	3.89 1 *
Retailing & Wholesaling	443	11.91	4.85	16.66 ¹
Industry Aggregate	2,190	17.70	3.08	21.06
South				
Banking, Insurance & Financial Services	129	14.02	9.04	$2.70^{-1} *$
Chemicals, Petroleum, Rubber & Plastic	211	41.32	18.36	$2.21^{-1}*$
Computer, IT & Internet Services	271	22.36	18.83	1.54 1 *
Industrial, Electric & Electronic Machinery	352	20.61	8.58	4.48^{-1}
Personal, Leisure & Business Services	519	22.88	10.38	6.85
Retailing & Wholesaling	496	20.61	13.61	3.33 1
Industry Aggregate	1,978	21.50	11.80	6.04
North				
Banking, Insurance & Financial Services	85	33.53	5.25	$1.73^{-1}*$
Chemicals, Petroleum, Rubber & Plastic	38	20.15	13.47	$1.20^{-1}*$
Computer, IT & Internet Services	350	19.45	1.63	11.37
Industrial, Electric & Electronic Machinery	227	25.05	17.89	3.87 1 *
Personal, Leisure & Business Services	278	23.79	0.35	9.79
Retailing & Wholesaling	217	15.43	5.98	6.08^{-1}
Industry Aggregate	1,195	21.05	1.15	8.76

^{* ...} improvement of the coefficient of variance is significant at the 0.05 level

 $N\dots$ number of analyzed transactions; $M\dots$ median of transaction multiples; $H\dots$ harmonic mean of transaction multiples; $V\dots$ coefficient of variance

Banking, Insurance & Financial Services 53 17.02 10.94 1.90 1.90 1.90	Central East				
Computer, IT & Internet Services	Banking, Insurance & Financial Services	53	17.02	10.94	1.90^{-1}
Industrial, Electric & Electronic Machinery 45 10.95 5.28 1.32 * Personal, Leisure & Business Services 101 11.31 7.68 3.23 * Personal, Leisure & Business Services 101 11.31 7.68 3.23 * Personal, Leisure & Business Services 155 11.55 0.08 3.68 * Personal, Leisure & Financial Services 496 11.39 0.17 3.72 * Personal, Leisure & Financial Services 69 14.98 6.83 6.10 Chemicals, Petroleum, Rubber & Plastic 96 11.49 8.27 1.46 * * Computer, IT & Internet Services 46 9.57 4.50 2.23 * * Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 * Personal, Leisure & Business Services 131 10.13 3.31 3.15 * Petroleum, Rubber & Plastic 679 11.34 3.84 4.72 * Personal, Leisure & Financial Services 11 15.58 55.07 2.24 * Personal, Leisure & Financial Services 11 15.58 55.07 2.24 * Personal, Leisure & Financial Services 11 15.58 16.57 1.69 * Personal, Leisure & Business Services 11 15.58 55.07 2.24 * Personal, Leisure & Business Services 11 15.58 16.57 1.69 * Personal, Leisure & Business Services 6 13.49 14.53 1.70 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Business Services 7 5.94 6.78 2.36 * Personal, Leisure & Financial Services 7 5.94 6.78 2.36 * Personal, Leisure & Financial Services 7 5.94 6.78 2.36 * Personal, Leisure & Financial Services 7 5.94	Chemicals, Petroleum, Rubber & Plastic	43	8.66	0.05	
Personal, Leisure & Business Services 101 11.31 7.68 3.23 1 1 1.55 11.55 0.08 3.68 1 1 1.31 1.35	Computer, IT & Internet Services	99	8.38	1.55	2.38^{-1}
Retailing & Wholesaling	Industrial, Electric & Electronic Machinery	45	10.95	5.28	
Industry Aggregate 496 11.39 0.17 3.72 South East Banking, Insurance & Financial Services 69 14.98 6.83 6.10 Chemicals, Petroleum, Rubber & Plastic 96 11.49 8.27 1.46 1* Computer, IT & Internet Services 46 9.57 4.50 2.23 1* Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 1 Personal, Leisure & Business Services 131 10.13 3.31 3.15 1 Retailing & Wholesaling 240 12.11 2.61 3.13 1 Industry Aggregate 679 11.34 3.84 4.72 East 11 15.58 55.07 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2	Personal, Leisure & Business Services	101	11.31	7.68	
South East Banking, Insurance & Financial Services 69 14.98 6.83 6.10 Chemicals, Petroleum, Rubber & Plastic 96 11.49 8.27 1.46 1* Computer, IT & Internet Services 46 9.57 4.50 2.23 1* Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 1 Personal, Leisure & Business Services 131 10.13 3.31 3.15 1 Retailing & Wholesaling 240 12.11 2.61 3.13 1 Industry Aggregate 679 11.34 3.84 4.72 East 8 11 15.58 55.07 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28	Retailing & Wholesaling	155	11.55	0.08	3.68 1
Banking, Insurance & Financial Services 69 14.98 6.83 6.10 Chemicals, Petroleum, Rubber & Plastic 96 11.49 8.27 1.46 1* Computer, IT & Internet Services 46 9.57 4.50 2.23 1* Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 1 Personal, Leisure & Business Services 131 10.13 3.31 3.15 1 Retailing & Wholesaling 240 12.11 2.61 3.13 1 Industry Aggregate 679 11.34 3.84 4.72 East 8 8 55.07 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28 9.27 8.60 2.03 1 <tr< td=""><td>Industry Aggregate</td><td>496</td><td>11.39</td><td>0.17</td><td>3.72</td></tr<>	Industry Aggregate	496	11.39	0.17	3.72
Chemicals, Petroleum, Rubber & Plastic 96 11.49 8.27 1.46 1* Computer, IT & Internet Services 46 9.57 4.50 2.23 1* Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 1 Personal, Leisure & Business Services 131 10.13 3.31 3.15 1 Retailing & Wholesaling 240 12.11 2.61 3.13 1 Industry Aggregate 679 11.34 3.84 4.72 East 3.89 11.34 3.84 4.72 East 55.07 2.24 1 2.24 1 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28 9.27 8.60 2.03 1 Industry	South East				
Computer, IT & Internet Services 46 9.57 4.50 2.23 1* Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 1 Personal, Leisure & Business Services 131 10.13 3.31 3.15 1 Retailing & Wholesaling 240 12.11 2.61 3.13 1 Industry Aggregate 679 11.34 3.84 4.72 East Banking, Insurance & Financial Services 11 15.58 55.07 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28 9.27 8.60 2.03 1 Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 72 9.38 8.64 3.70	Banking, Insurance & Financial Services	69	14.98	6.83	6.10
Computer, IT & Internet Services 46 9.57 4.50 2.23 1* Industrial, Electric & Electronic Machinery 97 14.23 7.20 2.49 1 Personal, Leisure & Business Services 131 10.13 3.31 3.15 1 Retailing & Wholesaling 240 12.11 2.61 3.13 1 Industry Aggregate 679 11.34 3.84 4.72 East Banking, Insurance & Financial Services 11 15.58 55.07 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28 9.27 8.60 2.03 1 Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 7 9.38 8.64	Chemicals, Petroleum, Rubber & Plastic	96	11.49	8.27	$1.46^{-1}*$
Personal, Leisure & Business Services 131 10.13 3.31 3.15 ¹ Retailing & Wholesaling 240 12.11 2.61 3.13 ¹ Industry Aggregate 679 11.34 3.84 4.72 East 8 11.34 3.84 4.72 Banking, Insurance & Financial Services 11 15.58 55.07 2.24 ¹ Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 ¹ Computer, IT & Internet Services 6 13.49 14.53 1.70 ¹ Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 ¹ Personal, Leisure & Business Services 7 5.94 6.78 2.36 ¹ Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 72 9.38 8.64 3.70 European Aggregate 623 20.58 0.67 3.44 ¹ * Chemicals, Petroleum, Rubber	Computer, IT & Internet Services	46	9.57	4.50	$2.23^{-1}*$
Retailing & Wholesaling 240 12.11 2.61 3.13 ¹ Industry Aggregate 679 11.34 3.84 4.72 East Banking, Insurance & Financial Services Banking, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 ¹ Computer, IT & Internet Services 6 13.49 14.53 1.70 ¹ Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 ¹ Personal, Leisure & Business Services 7 5.94 6.78 2.36 ¹ Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 8 9.27 8.60 2.03 ¹ Banking, Insurance & Financial Services 464 17.18 18.14 6.04 ¹ * Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 ¹ * Computer, IT & Internet Services 1,424 17.84 5.98 11.95 ¹ * Industrial, Electric &	Industrial, Electric & Electronic Machinery	97	14.23	7.20	
East 679 11.34 3.84 4.72 Banking, Insurance & Financial Services 11 15.58 55.07 2.24 ¹ Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 ¹ Computer, IT & Internet Services 6 13.49 14.53 1.70 ¹ Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 ¹ Personal, Leisure & Business Services 7 5.94 6.78 2.36 ¹ Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 72 9.38 8.64 3.70 European, Insurance & Financial Services 464 17.18 18.14 6.04 ¹ * Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 ¹ * Computer, IT & Internet Services 1,424 17.84 5.98 11.95 ¹ * Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.	Personal, Leisure & Business Services	131	10.13	3.31	
East Banking, Insurance & Financial Services 11 15.58 55.07 2.24 ¹ Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 ¹ Computer, IT & Internet Services 6 13.49 14.53 1.70 ¹ Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 ¹ Personal, Leisure & Business Services 7 5.94 6.78 2.36 ¹ Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 72 9.38 8.64 3.70 European, Insurance & Financial Services 464 17.18 18.14 6.04 ¹ * Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 ¹ * Computer, IT & Internet Services 1,424 17.84 5.98 11.95 ¹ * Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 ¹ *	Retailing & Wholesaling	240	12.11	2.61	3.13 1
Banking, Insurance & Financial Services 11 15.58 55.07 2.24 1 Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 1 Computer, IT & Internet Services 6 13.49 14.53 1.70 1 Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28 9.27 8.60 2.03 1 Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 72 9.38 8.64 3.70 European Aggregate 623 20.58 0.67 3.44 1* Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 1* Computer, IT & Internet Services 1,424 17.84 5.98 11.95 1* Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1*	Industry Aggregate	679	11.34	3.84	4.72
Chemicals, Petroleum, Rubber & Plastic 7 20.58 16.57 1.69 ¹ Computer, IT & Internet Services 6 13.49 14.53 1.70 ¹ Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 ¹ Personal, Leisure & Business Services 7 5.94 6.78 2.36 ¹ Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 72 9.38 8.64 3.70 European Aggregate 623 20.58 0.67 3.44 ¹* Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 ¹* Computer, IT & Internet Services 1,424 17.84 5.98 11.95 ¹* Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 ¹*	East				
Computer, IT & Internet Services 6 13.49 14.53 1.70 \(^{1}\) Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 \(^{1}\) Personal, Leisure & Business Services 7 5.94 6.78 2.36 \(^{1}\) Retailing & Wholesaling 28 9.27 8.60 2.03 \(^{1}\) Industry Aggregate 72 9.38 8.64 3.70 European Aggregate Banking, Insurance & Financial Services 464 17.18 18.14 6.04 \(^{1}\)* Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 \(^{1}\)* Computer, IT & Internet Services 1,424 17.84 5.98 11.95 \(^{1}\)* Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 \(^{1}\)*	Banking, Insurance & Financial Services	11	15.58	55.07	2.24^{-1}
Industrial, Electric & Electronic Machinery 13 3.89 4.36 3.00 1 Personal, Leisure & Business Services 7 5.94 6.78 2.36 1 Retailing & Wholesaling 28 9.27 8.60 2.03 1 Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 8	Chemicals, Petroleum, Rubber & Plastic	7	20.58	16.57	1.69 1
Personal, Leisure & Business Services 7 5.94 6.78 2.36 ¹ Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate Banking, Insurance & Financial Services 464 17.18 18.14 6.04 ¹ * Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 ¹ * Computer, IT & Internet Services 1,424 17.84 5.98 11.95 ¹ * Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 ¹ *	Computer, IT & Internet Services	6	13.49	14.53	1.70^{-1}
Retailing & Wholesaling 28 9.27 8.60 2.03 ¹ Industry Aggregate 72 9.38 8.64 3.70 European Aggregate 8 8 8 8 8 8 8 8 8 9.27 8 8 8 8 9 2 8 9 2 8 8 8 9 2 8 8 8 9 2 8 9 8 8	Industrial, Electric & Electronic Machinery	13	3.89	4.36	3.00^{-1}
Industry Aggregate 72 9.38 8.64 3.70 European Aggregate Banking, Insurance & Financial Services Banking, Insurance & Financial Services 464 17.18 18.14 6.04 1* Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 1* Computer, IT & Internet Services 1,424 17.84 5.98 11.95 1* Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1*		7	5.94	6.78	
European Aggregate 464 17.18 18.14 6.04 1 * Banking, Insurance & Financial Services 464 17.18 18.14 6.04 1 * Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 1 * Computer, IT & Internet Services 1,424 17.84 5.98 11.95 1 * Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1 *	Retailing & Wholesaling	28	9.27	8.60	2.03^{-1}
Banking, Insurance & Financial Services 464 17.18 18.14 6.04 1* Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 1* Computer, IT & Internet Services 1,424 17.84 5.98 11.95 1* Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1*	Industry Aggregate	72	9.38	8.64	3.70
Chemicals, Petroleum, Rubber & Plastic 623 20.58 0.67 3.44 1* Computer, IT & Internet Services 1,424 17.84 5.98 11.95 1* Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1*	European Aggregate				
Computer, IT & Internet Services 1,424 17.84 5.98 11.95 1 * Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1 *	Banking, Insurance & Financial Services	464	17.18	18.14	$6.04^{-1}*$
Industrial, Electric & Electronic Machinery 1,327 17.22 2.22 8.34 1*	Chemicals, Petroleum, Rubber & Plastic	623	20.58	0.67	
· · · · · · · · · · · · · · · · · · ·	Computer, IT & Internet Services	1,424	17.84	5.98	11.95 1 *
Personal Leisure & Rusiness Services 1 708 16 99 1 77 9 93 1 *	Industrial, Electric & Electronic Machinery				
	Personal, Leisure & Business Services	1,708	16.99	1.77	9.93 1 *
Retailing & Wholesaling 1,669 14.38 1.02 18.43	Retailing & Wholesaling	1,669	14.38		
Industry Aggregate 7,215 16.66 9.69 18.35					

^{1 ...} classification according to industry leads to a lower coefficient of variance compared to an aggregate calculation * ... improvement of the coefficient of variance is significant at the 0.05 level

Table 3: Analysis of the reliability of "DEV/EBIT" transaction multiples according to industry classification serving as peer group selection criterion (using the coefficient of variance V)

European Region / Industry Classification	N	M	Н	V
Central				
Banking, Insurance & Financial Services	62	19.39	7.63	5.76 1 *
Chemicals, Petroleum, Rubber & Plastic	48	27.11	19.75	$1.27^{-1}*$
Computer, IT & Internet Services	89	22.27	32.70	1.33 1 *
Industrial, Electric & Electronic Machinery	196	22.07	14.07	5.56 1 *
Personal, Leisure & Business Services	86	21.04	13.58	$2.67^{-1}*$
Retailing & Wholesaling	85	12.28	23.42	$6.48^{-1}*$
Industry Aggregate	566	20.93	15.23	13.35
West				
Banking, Insurance & Financial Services	100	17.85	12.84	6.73 1 *
Chemicals, Petroleum, Rubber & Plastic	158	43.70	53.78	5.33 1 *
Computer, IT & Internet Services	474	38.46	13.95	$6.06^{-1} *$
Industrial, Electric & Electronic Machinery	372	21.72	0.83	$6.58^{-1}*$
Personal, Leisure & Business Services	547	26.11	14.61	$7.82^{-1}*$
Retailing & Wholesaling	410	14.05	6.00	3.21 1 *
Industry Aggregate	2,061	24.71	3.48	14.24
South				

 $N\dots$ number of analyzed transactions; $M\dots$ median of transaction multiples; $H\dots$ harmonic mean of transaction multiples; $V\dots$ coefficient of variance

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Banking, Insurance & Financial Services	123	14.31	13.06	4.15	•'
Chemicals, Petroleum, Rubber & Plastic	150	29.67	18.77	1.20 1 *	
Computer, IT & Internet Services	232	44.67	16.48	3.31 1	
Industrial, Electric & Electronic Machinery	317	29.06	10.55	4.22 1	
Personal, Leisure & Business Services	444	25.73	14.74	3.64	
Retailing & Wholesaling	423	24.03	14.83	3.85	
Industry Aggregate	1,689	25.14	14.05	4.24	
North	1,002	23.17	14.03	7.27	•
Banking, Insurance & Financial Services	110	17.19	6.85	2.14 1 *	
Chemicals, Petroleum, Rubber & Plastic	38	30.15	17.14	4.06 1	
Computer, IT & Internet Services	311	22.03	1.60	3.06 1	
Industrial, Electric & Electronic Machinery	236	33.28	14.66	3.42	
Personal, Leisure & Business Services	287	27.20	13.14	3.65 1	
Retailing & Wholesaling	233	19.98	7.16	4.46 ¹	
Industry Aggregate Central East	1,215	25.12	4.83	4.78	
	00	20.05	9.50	4.32 1 *	
Banking, Insurance & Financial Services	90	20.05	8.52	1.65 1 *	
Chemicals, Petroleum, Rubber & Plastic	122	14.26	0.17	3.27 1 *	
Computer, IT & Internet Services	189	13.07	3.55	3.27 * 3.94 ¹ *	
Industrial, Electric & Electronic Machinery	100	15.71	1.73	3.94 *	
Personal, Leisure & Business Services	187	12.32	9.58	2.32 1 *	
Retailing & Wholesaling	345	16.07	0.25	3.03 1 *	
Industry Aggregate	1,033	15.10	0.50	8.42	
South East				1	
Banking, Insurance & Financial Services	92	12.18	5.70	3.46 1	
Chemicals, Petroleum, Rubber & Plastic	94	12.63	6.10	1.93 1 *	
Computer, IT & Internet Services	50	17.97	2.80	4.64	
Industrial, Electric & Electronic Machinery	102	19.97	8.19	3.60 1	
Personal, Leisure & Business Services	148	13.74	3.99	3.86^{-1}	
Retailing & Wholesaling	243	12.36	2.44	6.21	
Industry Aggregate	729	13.56	3.67	5.27	
East					
Banking, Insurance & Financial Services	91	252.49	8.85	$1.70^{-1}*$	
Chemicals, Petroleum, Rubber & Plastic	195	9.14	1.09	10.85	
Computer, IT & Internet Services	79	14.04	4.22	8.37 1	
ndustrial, Electric & Electronic Machinery	125	9.63	2.28	3.41 1 *	
Personal, Leisure & Business Services	289	10.15	3.33	14.98	
Retailing & Wholesaling	471	18.55	6.02	11.77	
Industry Aggregate	1,250	13.76	2.38	11.56	
European Aggregate					•
	668	18.16	4.65	$5.00^{-1} *$	
Banking, Insurance & Financial Services	000				
				8.21 1 *	
Chemicals, Petroleum, Rubber & Plastic	805	17.49	1.55	8.21 ¹ * 29.35	
Chemicals, Petroleum, Rubber & Plastic Computer, IT & Internet Services	805 1,424	17.49 25.19	1.55 8.22	29.35	
Chemicals, Petroleum, Rubber & Plastic Computer, IT & Internet Services Industrial, Electric & Electronic Machinery	805 1,424 1,448	17.49 25.19 21.42	1.55 8.22 2.30	29.35 11.45 ¹ *	
Banking, Insurance & Financial Services Chemicals, Petroleum, Rubber & Plastic Computer, IT & Internet Services Industrial, Electric & Electronic Machinery Personal, Leisure & Business Services Retailing & Wholesaling	805 1,424	17.49 25.19	1.55 8.22	29.35	

^{1 ...} classification according to industry leads to a lower coefficient of variance compared to an aggregate calculation

4.2 Firm size serving as a peer group selection criterion: its impact on the reliability of transaction multiples

Some business appraisers apply the firm size as another primary selection criterion. The classification of the size of a privately held business itself can be based on different criteria, especially the (operating) sales, the sum of the balance sheet or the number of employees. In doing so, it is usually found helpful to place a size restriction of no more than 10 to 25 times the sales volume of the target business (Trugman, 2012). In the analysis shown in tables 4 to 6(each table again shows the calculation of one of the three different types of regarded transaction multiples) the classification is based on the operating sales following the recommended size classification of the European Union 2003/361/EG, dividing businesses into small, medium and large sized businesses. The T-test shows the intensity of improvement of the firm size-related transaction multiples instead of an aggregate calculation.

^{* ...} improvement of the coefficient of variance is significant at the 0.05 level

 $N\ldots$ number of analyzed transactions; $M\ldots$ median of transaction multiples; $H\ldots$ harmonic mean of transaction multiples; $V\ldots$ coefficient of variance

Moreover, the analysis indicates that the classification of the transaction multiples according to the firm size in most cases leads to a lower coefficient of variance (see the "1" behind the coefficient of variance). Transaction multiples that are based on a firm size classification of the comparable businesses therefore are more reliable. This is empirical evidence that also justifies the size classification as a (primary) selection criterion for the assessment of comparability. The same was found in an analysis conducted by Grbenic and Zunk (2012) for the Central European countries Austria, Germany and Switzerland. The results also show that the improvement in many cases is significant (marked with an asterisk behind the coefficient of variance).

Table 4: Analysis of the reliability of "DEV/Sales" transaction multiples according to firm size serving as peer group selection criterion (using the coefficient of variance V)

European Region / Firm Size	N	M	Н	V
Central				
Small Sized Enterprises	448	20.41	1.57	$9.48^{-1}*$
Medium Sized Enterprises	301	4.65	4.08	$2.03^{-1}*$
Large Sized Enterprises	552	1.32	0.54	2.96 1 *
Firm Size Aggregate	1,301	3.40	0.94	15.48
West				
Small Sized Enterprises	940	17.04	2.11	12.93 1 *
Medium Sized Enterprises	828	4.09	1.38	18.62 1
Large Sized Enterprises	1,661	1.46	0.66	$2.87^{-1} *$
Firm Size Aggregate	3,429	3.01	0.96	24.59
South				
Small Sized Enterprises	1,025	47.50	2.92	6.08 1 *
Medium Sized Enterprises	570	3.21	0.95	$2.60^{-1} *$
Large Sized Enterprises	1,637	3.76	1.57	$2.99^{-1}*$
Firm Size Aggregate	3,232	7.15	1.62	10.24
North				
Small Sized Enterprises	2,182	22.67	1.30	8.80 1
Medium Sized Enterprises	642	5.68	0.11	9.25 1
Large Sized Enterprises	827	2.47	0.86	3.83 1 *
Firm Size Aggregate	3,651	9.45	0.42	11.02
Central East				
Small Sized Enterprises	841	3.24	2.33	10.33
Medium Sized Enterprises	442	0.99	0.25	3.94 1 *
Large Sized Enterprises	438	0.89	0.02	1.11 1 *
Firm Size Aggregate	1,721	1.46	0.08	14.22
South East				
Small Sized Enterprises	634	3.41	0.87	20.54 1 *
Medium Sized Enterprises	184	1.08	0.01	$2.09^{-1}*$
Large Sized Enterprises	385	0.74	1.36	3.23 1 *
Firm Size Aggregate	1,203	1.52	0.01	28.28
East				1
Small Sized Enterprises	635	4.18	0.29	3.99 1
Medium Sized Enterprises	304	1.18	1.60	2.83 1 *
Large Sized Enterprises	715	1.26	0.06	$2.02^{-1}*$
Firm Size Aggregate	1,654	1.57	0.12	6.21
European Aggregate				i
Small Sized Enterprises	6,705	13.48	1.11	30.06 1 *
Medium Sized Enterprises	3,271	2.59	0.03	24.02 1 *
Large Sized Enterprises	6,215	1.73	1.01	3.47 1 *
Firm Size Aggregate	16,191	3.51	0.15	46.26

^{1 ...} classification according to size of the business leads to a lower coefficient of variance compared to an aggregate

^{* ...} improvement of the coefficient of variance is significant at the 0.05 level

 $N\ldots$ number of analyzed transactions; $M\ldots$ median of transaction multiples; $H\ldots$ harmonic mean of transaction multiples; $V\ldots$ coefficient of variance

Table 5: Analysis of the reliability of "DEV/EBITDA" transaction multiples according to firm size serving as peer group selection criterion (using the coefficient of variance V)

European Region / Firm Size	N	M	Н	V
Central	11	141	11	<u> </u>
Small Sized Enterprises	74	33.45	17.41	5.81 1 *
Medium Sized Enterprises	122	15.50	16.61	2.88 1 *
Large Sized Enterprises	409	12.56	9.33	1.65 1 *
Firm Size Aggregate	605	14.75	10.91	15.99
	003	14.73	10.91	13.99
West	205	24.10	12.61	10.00 1 *
Small Sized Enterprises	295	34.10	13.61	$10.06^{-1} * 3.02^{-1} *$
Medium Sized Enterprises	474	25.99 13.85	6.90 2.29	3.02 * 3.55 ¹ *
Large Sized Enterprises	1,421			
Firm Size Aggregate	2,190	17.70	3.08	21.06
South				1 .
Small Sized Enterprises	333	46.66	10.78	3.13 1 *
Medium Sized Enterprises	433	21.04	10.91	1.68 1 *
Large Sized Enterprises	1,212	19.54	12.49	6.98
Firm Size Aggregate	1,978	21.50	11.80	6.04
North				
Small Sized Enterprises	437	26.69	2.29	6.04 1
Medium Sized Enterprises	306	23.50	0.39	$2.93^{-1}*$
Large Sized Enterprises	452	17.79	7.65	$1.72^{-1}*$
Firm Size Aggregate	1,195	21.05	1.15	8.76
Central East				
Small Sized Enterprises	216	14.27	4.47	3.41^{-1}
Medium Sized Enterprises	118	11.03	6.78	2.20^{-1}
Large Sized Enterprises	162	10.51	0.06	2.85^{-1}
Firm Size Aggregate	496	11.39	0.17	3.72
South East				
Small Sized Enterprises	343	11.39	3.11	6.18
Medium Sized Enterprises	119	10.34	3.93	2.36^{-1}
Large Sized Enterprises	217	12.01	5.98	3.36 1
Firm Size Aggregate	679	11.34	3.84	4.72
East				
Small Sized Enterprises	29	41.33	17.62	2.64^{-1}
Medium Sized Enterprises	15	15.58	10.64	3.26
Large Sized Enterprises	28	6.95	5.31	$0.90^{-1}*$
Firm Size Aggregate	72	9.38	8.64	3.70
European Aggregate	, 2	. .		
Small Sized Enterprises	1,727	22.69	5.55	12.33 1 *
Medium Sized Enterprises Medium Sized Enterprises	1,587	19.00	1.66	3.23 1 *
Large Sized Enterprises	3,901	14.81	1.94	8.03 1 *
Firm Size Aggregate	7,215	16.66	9.69	18.35
1 classification according to size of the business				

^{1 ...} classification according to size of the business leads to a lower coefficient of variance compared to an aggregate calculation

^{* ...} improvement of the coefficient of variance is significant at the 0.05 level

 $N\dots$ number of analyzed transactions; $M\dots$ median of transaction multiples; $H\dots$ harmonic mean of transaction multiples; $V\dots$ coefficient of variance

Table 6: Analysis of the reliability (coefficient of variance) of "DEV/EBIT" transaction multiples according to firm size serving as peer group selection criterion (using the coefficient of variance V)

European Region / Firm Size	N	M	Н	V
Central				
Small Sized Enterprises	69	51.63	17.14	5.63 1 *
Medium Sized Enterprises	114	18.97	20.26	$2.60^{-1}*$
Large Sized Enterprises	383	17.44	13.92	$7.43^{-1}*$
Firm Size Aggregate	566	20.93	15.23	13.35
West				
Small Sized Enterprises	260	47.58	18.72	5.38 1 *
Medium Sized Enterprises	448	33.23	8.89	$7.16^{-1}*$
Large Sized Enterprises	1,353	19.91	2.56	$4.11^{-1}*$
Firm Size Aggregate	2,061	24.71	3.48	14.24
South				
Small Sized Enterprises	291	66.89	14.11	3.11 1
Medium Sized Enterprises	389	40.40	16.30	3.29^{-1}
Large Sized Enterprises	1,009	20.14	13.33	4.86
Firm Size Aggregate	1,689	25.14	14.05	4.24
North				_
Small Sized Enterprises	414	37.03	2.40	4.08^{-1}
Medium Sized Enterprises	274	25.09	13.67	3.13 1
Large Sized Enterprises	527	21.84	8.89	3.86 1
Firm Size Aggregate	1,215	25.12	4.83	4.78
Central East				_
Small Sized Enterprises	328	18.09	12.68	$3.74^{-1}*$
Medium Sized Enterprises	316	14.69	2.48	$3.02^{-1}*$
Large Sized Enterprises	389	14.97	0.18	8.44
Firm Size Aggregate	1,033	15.10	0.50	8.42
South East				
Small Sized Enterprises	342	16.75	3.20	4.44
Medium Sized Enterprises	135	12.05	6.87	$2.01^{-1} *$
Large Sized Enterprises	252	10.66	3.50	6.92
Firm Size Aggregate	729	13.56	3.67	5.27
East				
Small Sized Enterprises	375	33.46	2.16	11.14^{-1}
Medium Sized Enterprises	201	17.76	31.43	$2.81^{-1}*$
Large Sized Enterprises	674	9.85	1.93	$4.53^{-1}*$
Firm Size Aggregate	1,250	13.76	2.38	11.56
European Aggregate				
Small Sized Enterprises	2,079	28.53	4.47	19.30
Medium Sized Enterprises	1,877	21.61	7.58	8.87 1 *
Large Sized Enterprises	4,587	16.37	4.31	7.16 ¹ *
Firm Size Aggregate	8,543	19.37	24.28	18.82
1 electification according to size of the business leads to				

 $^{1 \}dots$ classification according to size of the business leads to a lower coefficient of variance compared to an aggregate calculation

In addition to the finding that the classification of the businesses according to their size can improve the reliability of the transaction multiples, the data analysis also shows that smaller businesses are regularly sold at higher transaction multiples than larger businesses. This is remarkable in so far as both the valuation theorists and business appraisers are trying to find any size-related empirical evidence that would allow for a data based reduction of the (fair) market value of small and medium sized enterprises.

^{* ...} improvement of the coefficient of variance is significant at the 0.05 level

 $N\ldots$ number of analyzed transactions; $M\ldots$ median of transaction multiples; $H\ldots$ harmonic mean of transaction multiples; $V\ldots$ coefficient of variance

Exemplarily, the Morningstar Studies and the Duff & Phelps Studies conducted with data from the US stock market provide empirical evidence (Pratt and Grabowski, 2010). Therein the proposed methods are (i) the adjustment of the beta, in view of the weaker or even lacking capability of the owner of a smaller business to diversify his investment, in the form of the total beta or in the form of a combination of the standard and the total beta (Kerins, Smith and Smith, 2004; Damodaran, 2006; Balz and Bordemann, 2007), (ii) the modification of the Capital Asset Pricing Model by integrating a size premium to take into consideration the higher risk of smaller businesses (Schulz, 2009) or(iii) to raise the market risk premium as a result of the reduced leverage of the owner of a smaller business and/or as a result of the higher cost of equity (Knoll, 2010). The justification of all these efforts is said to be found in the facts that (i) different sizes of businesses lead to different growth rates and as a result of that regularly to higher risks for smaller businesses, that (ii) smaller businesses usually show a poorer cost structure, that (iii) the management of smaller businesses is less professional and effective, that(iv) smaller businesses face a poorer diversification of products and markets and that (v) larger businesses often diversify by doing their business in several markets and/or industries (Pratt, 2005; Damodaran, 2010).

The finding that smaller businesses sell at higher transaction multiples than larger businesses leads to the conclusion that the transaction prices and hence also the transaction multiples generated for smaller businesses reflect a larger number of effects on the transaction price than there are reflected for larger businesses. Compared to the United States of America where it is believed that smaller companies in most industries tend to sell at lower transaction multiples of most financial value drivers than larger companies, this is an interesting finding (Pratt, 2005). While the transaction multiples of larger businesses especially reflect financial effects covered by the cash flow, the transaction multiples of smaller businesses also reflect non-financial factors. This empirical evidence leads to further conclusions: (i) the (fair) market values calculated in accordance with the nowadays used valuation methods provide a far poorer validity for smaller businesses than for larger businesses, (ii) the size of the business has to be taken into consideration when forming the peer group and (iii) the target business and the comparable businesses have to belong at least to the same sizeclass.

4.3 Improvement of the reliability of transaction multiples through a combination of industry classification and firm size as peer group selection criteria

On the basis of the presented results either the industry classification or the size classification of the business can improve the reliability of the calculated transaction multiples. For that reason, it is also tested if the combination of the two classification criteria leads to the highest reliability of the transaction multiples. The results for the six specified industries presented for small sized enterprises(table 7), medium sized enterprises(table 8), for large sized enterprises (table 9) and additionally for the "firm size aggregate" (in tables 7 to 9) show the median, the harmonic mean and the coefficient of variance of the calculated transaction multiples (solely for the DEV/Sales Multiple). The results of the T-test indicate whether the improvement of the coefficient of variance is significant on the 5 % level of significance. The analysis shows that the combination of the industry classification and the size classification can - in most cases - improve the reliability of the calculated transaction multiples. The coefficient of variance marked with a "3" shows an improvement compared with both classification criteria, a "2" shows an improvement compared with the size classification solely and a "1" shows an improvement compared with the industry classification solely. Transaction multiples that are based on both industry classification and size classification of the comparable businesses in these cases are most reliable. There is empirical evidence that both the industry classification and the size classification have to be used in combination as (primary) selection criteria for the comparable businesses.

When using both selection criteria - industry classification and firm size - simultaneously the improvement of the reliability of the transaction multiple is in many cases significant (marked with a triple asterisk behind the coefficient of variance) than either using only the industry classification (marked with an asterisk behind the coefficient of variance) or only the firm size as classification criterion (marked with a double asterisk behind the coefficient of variance).

Table 7: Analysis of the reliability of "DEV/Sales" transaction multiples according to the combination of industry classification and firm size serving as peer group selection criteria for small sized enterprises (using the coefficient of variance V)

(using the coefficient				
European Region / Industry Classification	N	M	Н	V
Central				
Banking, Insurance & Financial Services	73	16.82	14.95	10.17^{-1}
Chemicals, Petroleum, Rubber & Plastic	30	229.45	21.24	$2.95^{-3} **$
Computer, IT & Internet Services	92	14.20	0.42	$2.14^{-3} **$
Industrial, Electric & Electronic Machinery	80	14.05	2.90	$2.21^{-3}**$
Personal, Leisure & Business Services	150	38.32	4.98	$3.62^{-3}**$
Retailing & Wholesaling	23	5.57	1.65	3.27 3 ***
Industry Aggregate	448	20.41	1.57	9.48
West				,,,,
Banking, Insurance & Financial Services	119	98.54	23.88	4.59 1 **
Chemicals, Petroleum, Rubber & Plastic	43	42.41	2.46	2.40 3 ***
Computer, IT & Internet Services	275	5.75	2.06	3.97 ³ **
Industrial, Electric & Electronic Machinery	130	11.87	5.48	4.47 ³ ***
Personal, Leisure & Business Services	232	18.65	1.05	15.04
Retailing & Wholesaling	142	28.36	2.90	3.16 3 ***
	940	28.30 17.04	2.90	12.93
Industry Aggregate	940	17.04	2.11	12.93
South	220	7645	10.40	2.99 3 **
Banking, Insurance & Financial Services	229	76.45	10.49	2.99 3 **
Chemicals, Petroleum, Rubber & Plastic	43	13.06	61.05	5.30 3 *
Computer, IT & Internet Services	168	11.63	1.87	4.67 3
Industrial, Electric & Electronic Machinery	133	40.41	4.70	4.68 3
Personal, Leisure & Business Services	241	26.35	2.38	4.25^{-3}
Retailing & Wholesaling	211	147.13	1.92	8.44 3 *
Industry Aggregate	1,025	47.50	2.92	6.08
North				
Banking, Insurance & Financial Services	245	44.73	27.10	10.46^{-1}
Chemicals, Petroleum, Rubber & Plastic	44	67.96	4.10	1.95 3 **
Computer, IT & Internet Services	497	9.17	0.41	$3.45^{-3} **$
Industrial, Electric & Electronic Machinery	411	34.06	4.38	3.50 3 **
Personal, Leisure & Business Services	697	22.12	4.35	5.05 3 **
Retailing & Wholesaling	288	35.42	1.33	$4.08^{-3} **$
Industry Aggregate	2,182	22.67	1.30	8.80
Central East				
Banking, Insurance & Financial Services	130	14.53	2.33	7.04^{-3}
Chemicals, Petroleum, Rubber & Plastic	52	4.35	0.90	$2.27^{-3}**$
Computer, IT & Internet Services	191	2.90	0.66	4.58 3 **
Industrial, Electric & Electronic Machinery	74	2.97	0.79	2.12 3 **
Personal, Leisure & Business Services	200	2.05	2.17	3.08 3 **
Retailing & Wholesaling	194	2.32	0.55	3.37 ³ **
Industry Aggregate	841	3.24	2.33	10.33
South East	071	J.4T	2.33	10,55
Banking, Insurance & Financial Services	101	26.38	28.93	2.94 3 **
Chemicals, Petroleum, Rubber & Plastic	51	26.38	28.93 1.50	2.94^{-3}
	40			4.41 ³ **
Computer, IT & Internet Services		4.00	0.95	2.98 ³ **
Industrial, Electric & Electronic Machinery	104	2.97	1.14	2.98 ³ ** 11.95 ³ **
Personal, Leisure & Business Services	146	3.23	0.82	4.87 ³ **
Retailing & Wholesaling	192	1.79	0.51	
Industry Aggregate	634	3.41	0.87	20.54
East				2
Banking, Insurance & Financial Services	89	74.16	0.29	2.40^{-3}
Chemicals, Petroleum, Rubber & Plastic	25	8.48	1.20	$3.47^{\frac{3}{3}}*$
Chemicals, Petroleum, Rubber & Plastic Computer, IT & Internet Services	25 33	5.05	0.75	3.77^{-3}
Chemicals, Petroleum, Rubber & Plastic	25			3.47 ³ * 3.77 ³ 2.19 ³ 3.90 ³

Retailing & Wholesaling	215	2.43	0.26	3.85^{-3}
Industry Aggregate	635	4.18	0.29	3.99
European Aggregate				_
Banking, Insurance & Financial Services	986	66.56	2.61	13.13 3 **
Chemicals, Petroleum, Rubber & Plastic	288	11.85	2.04	$4.47^{-3} *$
Computer, IT & Internet Services	1,296	7.33	0.90	$4.36^{3}**$
Industrial, Electric & Electronic Machinery	988	14.83	1.49	$5.20^{-3} **$
Personal, Leisure & Business Services	1,882	12.80	1.29	28.11 3 *
Retailing & Wholesaling	1,265	7.12	0.64	6.97 3 **
Industry Aggregate	6,705	13.48	1.11	30.06

^{1 ...} improvement compared with the industry classification only; 2 ... improvement compared with the size classification only; 3 ... improvement compared with both classification

Table 8: Analysis of the reliability of "DEV/Sales" transaction multiples according to the combination of industry classification and firm size serving as peer group classification criteria for medium sized enterprises (using the coefficient of variance V)

European Region / Industry Classification	N	M	Н	V
Central				
Banking, Insurance & Financial Services	35	15.44	6.30	1.21 3 *
Chemicals, Petroleum, Rubber & Plastic	13	2.46	1.48	1.57 3 *
Computer, IT & Internet Services	76	2.27	1.67	2.49^{-1}
Industrial, Electric & Electronic Machinery	77	2.95	1.47	2.09^{-1}
Personal, Leisure & Business Services	71	6.02	1.97	1.93 ³ *
Retailing & Wholesaling	29	35.72	0.39	$0.75^{-3} *$
Industry Aggregate	301	4.65	4.08	2.03
West				
Banking, Insurance & Financial Services	44	22.56	7.43	2.36 3 ***
Chemicals, Petroleum, Rubber & Plastic	74	23.09	2.04	1 35 ³ ***
Computer, IT & Internet Services	179	2.48	1.35	$2.61^{-3}***$
Industrial, Electric & Electronic Machinery	148	2.99	1.20	$1.90^{-3}***$
Personal, Leisure & Business Services	221	6.34	1.29	$2.08^{-3}***$
Retailing & Wholesaling	162	3.59	1.22	11.57 3 **
Industry Aggregate	828	4.09	1.38	18.62
South				
Banking, Insurance & Financial Services	59	10.68	3.44	2.66^{-1}
Chemicals, Petroleum, Rubber & Plastic	29	3.12	1.86	$2.16^{-3} *$
Computer, IT & Internet Services	98	5.69	0.71	1.33 3 *
Industrial, Electric & Electronic Machinery	126	2.50	1.04	$2.74^{-1} *$
Personal, Leisure & Business Services	128	2.76	0.61	2.13 3 *
Retailing & Wholesaling	130	1.46	1.31	3.47 1 *
Industry Aggregate	570	3.21	0.95	2.60
North				
Banking, Insurance & Financial Services	39	11.76	1.44	1.87 3 ***
Chemicals, Petroleum, Rubber & Plastic	16	11.62	6.75	1.19 3 **
Computer, IT & Internet Services	159	3.42	1.40	2.20 3 **
Industrial, Electric & Electronic Machinery	84	2.62	1.08	3.06 3 **
Personal, Leisure & Business Services	219	5.32	0.04	7.13^{-2}
Retailing & Wholesaling	125	11.61	0.86	1.31 3 **
Industry Aggregate	642	5.68	0.11	9.25
Central East				
Banking, Insurance & Financial Services	40	4.22	1.82	2.46 3 *
Chemicals, Petroleum, Rubber & Plastic	58	0.70	0.85	2.67^{-3}

^{* ...} improvement compared with the industry classification is only significant at a 0.05 level; ** ... improvement compared with the size classification is only significant at the 0.05 level; *** ... improvement compared with both industry and size classification is significant at the 0.05 level

 $N\ldots$ number of analyzed transactions; $M\ldots$ median of transaction multiples; $H\ldots$ harmonic mean of transaction multiples; $V\ldots$ coefficient of variance

Computer, IT & Internet Services 68 1.18 0.07 1.11 3 *** Industrial, Electric & Electronic Machinery 68 0.83 0.51 2.07 3 Personal, Leisure & Business Services 60 0.71 0.65 1.22 3 *** Retailing & Wholesaling 148 1.05 0.31 2.16 3 * Industry Aggregate 442 0.99 0.25 3.94 South East Banking, Insurance & Financial Services 26 19.38 0.11 0.82 3 * Chemicals, Petroleum, Rubber & Plastic 21 0.72 0.48 1.96 3 * Computer, IT & Internet Services 13 1.69 0.30 0.93 3 * Industrial, Electric & Electronic Machinery 35 0.93 0.01 1.79 3 Personal, Leisure & Business Services 35 1.80 0.85 0.93 3 * Retailing & Wholesaling 54 0.70 0.45 2.59 1 * Industry Aggregate 184 1.08 0.01 2.09 East Industry Aggregate </th
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Retailing & Wholesaling 75 0.80 0.95 2.61 3 *
<i>Industry Aggregate</i> 304 1.18 1.60 2.83
European Aggregate
Banking, Insurance & Financial Services 315 10.68 2.96 3.02 3 ***
Chemicals, Petroleum, Rubber & Plastic 247 1.62 1.04 2.34 3 ***
Computer, IT & Internet Services 605 2.29 0.42 2.36 3 ***
Industrial, Electric & Electronic Machinery 582 1.74 0.01 3.35 3 ***
Personal, Leisure & Business Services 799 3.64 0.13 9.01 3 ***
Retailing & Wholesaling 723 1.71 0.88 22.96 1
<i>Industry Aggregate</i> 3,271 2.59 0.03 24.02

^{1 ...} improvement compared with the industry classification only; 2 ... improvement compared with the size classification only; 3 ... improvement compared with both classification

Table 9: Analysis of the reliability of "DEV/Sales" transaction multiples according to the combination of industry classification and firm size serving as peer group classification criteria for large sized enterprises (using the coefficient of variance V)

European Region / Industry Classification	N	M	Н	V
Central				
Banking, Insurance & Financial Services	30	2.06	1.36	$2.48^{-1} *$
Chemicals, Petroleum, Rubber & Plastic	68	4.93	0.96	$1.42^{-3} *$
Computer, IT & Internet Services	65	1.81	1.93	$0.97^{-3}***$
Industrial, Electric & Electronic Machinery	212	1.32	0.58	3.90
Personal, Leisure & Business Services	76	1.30	0.38	$1.47^{-3} *$
Retailing & Wholesaling	101	0.66	0.30	$2.19^{-3} *$
Industry Aggregate	552	1.32	0.54	2.96
West				
Banking, Insurance & Financial Services	63	11.25	2.62	1.95 3 *
Chemicals, Petroleum, Rubber & Plastic	150	2.72	0.16	$2.09^{-3} *$
Computer, IT & Internet Services	334	1.46	1.01	1.89 3 *
Industrial, Electric & Electronic Machinery	293	1.32	0.16	$2.26^{-3} *$
Personal, Leisure & Business Services	464	1.52	0.66	$2.39^{-3} *$
Retailing & Wholesaling	357	1.02	0.60	$2.46^{-3} *$
Industry Aggregate	1,661	1.46	0.66	2.87

^{* ...} improvement compared with the industry classification is only significant at a 0.05 level; ** ... improvement compared with the size classification is only significant at the 0.05 level; *** ... improvement compared with both industry classification and firm size is significant at the 0.05 level

 $N\dots$ number of analyzed transactions; $M\dots$ median of transaction multiples; $H\dots$ harmonic mean of transaction multiples; $V\dots$ coefficient of variance

South Banking, Insurance & Financial Services 114 20.27 5.70 1.33 3 ** Chemicals, Petroleum, Rubber & Plastic 231 4.19 1.54 1.31 3 * Computer, IT & Internet Services 125 1.93 0.79 1.52 3 * Industrial, Electric & Electronic Machinery 346 3.74 1.50 2.25 3 * Personal, Leisure & Business Services 397 9.97 3.92 3.62 1 * Retailing & Wholesaling 424 2.80 1.12 1.73 3 * Industry Aggregate 1,637 3.76 1.57 2.99 North Banking, Insurance & Financial Services 37 4.97 7.08 0.71 3 *** Chemicals, Petroleum, Rubber & Plastic 26 2.48 2.21 1.77 3 Computer, IT & Internet Services 161 1.14 0.32 7.52 Industrial, Electric & Electronic Machinery 263 2.93 4.48 1.79 3 * Personal, Leisure & Business Services 133 1.98 1.64 1.46 3 *** Retailing & Wholesaling 207 2.27 0.70 1.99 3 *
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Banking, Insurance & Financial Services 27 2.89 1.46 0.50 ³ *
Chemicals, Petroleum, Rubber & Plastic 69 0.78 0.01 1.39
Computer, IT & Internet Services 43 1.67 21.31 0.69 *
Industrial, Electric & Electronic Machinery Personal, Leisure & Business Services 30 0.93 0.37 0.63 3 * 0.91 1.05 3 *
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Industry Aggregate 438 0.89 0.02 1.11
South East
Banking, Insurance & Financial Services 60 0.01 0.06 2.48 ³
Chemicals, Petroleum, Rubber & Plastic 73 0.49 0.32 1.25 3 ***
Computer, IT & Internet Services 31 1.24 0.82 1.01 3 ***
Industrial, Electric & Electronic Machinery 20 1.11 3.11 0.99 3 ***
Personal, Leisure & Business Services 33 1.43 0.23 1.09 3 ***
Retailing & Wholesaling 168 0.77 0.57 4.17 1
Industry Aggregate 385 0.74 1.36 3.23
East
Banking, Insurance & Financial Services 20 1.69 0.01 0.91 3 *
Chemicals, Petroleum, Rubber & Plastic 158 1.22 0.21 1.27 ³ *
Computer, IT & Internet Services 46 1.89 0.72 1.42 ³ *
Industrial, Electric & Electronic Machinery 68 0.65 0.24 1.99 ³
Personal, Leisure & Business Services 132 0.86 0.28 1.91 3 *
Retailing & Wholesaling 291 1.95 0.06 1.78 ³ *
<i>Industry Aggregate</i> 715 1.26 0.06 2.02
European Aggregate
Banking, Insurance & Financial Services 351 3.77 0.03 2.23 ³ *
Chemicals, Petroleum, Rubber & Plastic 775 2.10 0.10 2.45 ³ *
Computer, IT & Internet Services 805 1.49 0.71 8.73
Industrial, Electric & Electronic Machinery 1,232 1.88 0.43 2.81 3 *
Personal, Leisure & Business Services 1,281 1.91 0.73 3.31 ³ *
Retailing & Wholesaling 1,771 1.42 0.10 3.18 ³ *
<i>Industry Aggregate</i> 6,215 1.73 1.01 3.47

^{1 ...} improvement compared with the industry classification only; 2 ... improvement compared with the size classification only; 3 ... improvement compared with both classification

^{* ...} improvement compared with the industry classification is only significant at a 0.05 level; ** ... improvement compared with the size classification is only significant at the 0.05 level; *** ... improvement compared with both industry classification and firm size is significant at the 0.05 level

 $N\dots$ number of analyzed transactions; $M\dots$ median of transaction multiples; $H\dots$ harmonic mean of transaction multiples; $V\dots$ coefficient of variance

5. Conclusion

As far as the formation of comparable peer groups is concerned, the results presented in this paper provide insights into the influence of the peer group selection criterion firm size on the reliability of transaction multiples, which are used to value privately held businesses. To contribute to the existing knowledge about the influence of peer group selection criteria on the reliability of the widely applied transaction multiples "DEV/Sales", "DEV/EBITDA" and "DEV/EBIT", three different cases were studied. Therefore, real data from European countries that deliver a statistically sufficient number of transaction data were analyzed (tables 1 to 9). In the first case, the influence that industry classification as single peer group selection criterion has on the reliability of the selected transaction multiples (table 1, 2 and 3) was analyzed. Then, the influence that the single peer group selection criterion firm size has on the reliability of the amount of the value of the transaction multiples "DEV/Sales", "DEV/EBITDA" and "DEV/EBIT" was investigated (table 4, 5 and 6). The results of the analysis in the third case were derived from a combination of the single criteria industry classification and firm size and were presented separately for small (table 7), medium (table 8) and large sized enterprises (table 9).

The findings indicate that using the peer group selection criterion firm size has an impact on the reliability of the transaction multiples. Furthermore, the results demonstrate that the combination of the peer group selection criteria industry classification and firm size lead to the most reliable transaction multiples to value privately held businesses. According to the results of this study, business valuation professionals as well as business appraisers should take the industry classification and firm size into account when they want to optimize the reliability of the calculated transaction multiples.

However, the presented study clearly has some limitations. Since there is no public centralized mechanism for collecting and making transaction price information available, the results of the analysis depend on the quality of the transaction data registered in mergers and acquisitions data bases. These circumstances especially have an influence on the dispersion of the calculated transaction multiples as well as on the skewness of the distribution presented in tables 1 to 9. Furthermore, it is noteworthy that this paper's calculation of the presented transaction multiples "DEV/Sales", "DEV/EBITDA" and DEV/EBIT" are based on present day data from ZEPHYR data base. The future validity of this analysis may therefore need an annual revision.

This paves the road for future research. Future studies should especially examine the impact of additional single peer group selection criteria and of their interdependencies. This could further improve the reliability of the calculated transaction multiples and subsequently the valuation of privately held businesses. Moreover, an extension of the peer group selection criteria base (i.e. the use of criteria in addition to the industry classification and the firm size) could be a promising contribution to the literature, particularly as far as knowledge about their impact on the reliability of the calculated transaction multiples is concerned. These transaction multiples could be made publicly available in a quantitative data base. Such a contribution would eventually allow for the creation of a computerized method that measures the degree of comparability of businesses. Thus it would help to answer the question if businesses should be added to the peer group or not.

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